

## CLAIMS

1. A method of synchronizing a plurality of clocks at different locations using a third clock (clock B) comprising the steps of:

5 determining a correction term,  $\varepsilon^A$  for a first one of the plurality of clocks (clock A) the correction term being the difference between the computed arrival time of a signal from clock B to clock A if clock A was synchronized to clock B, defined as  $s_1^A$ , minus the observed time by clock A of arrival of the signal from clock B at clock A;

10 determining a correction term,  $\varepsilon^C$  for any selected one or ones of the plurality of clocks (clocks C) to be synchronized, the correction term being the difference between the computed arrival time of a signal from clock B to clock C if clock C was synchronized to clock B, defined as  $s_2^A$  minus the observed time by clock C of arrival of the signal from clock B at clock C;

15 applying the difference between the correction terms,  $\varepsilon^A$  and  $\varepsilon^C$ , defining a correction term,  $\varepsilon^{CA}$  for clock C, to synchronize the selected one or ones of the plurality of clocks C for which  $\varepsilon^C$  has been determined, to clock A.

2. The method of claim 1 wherein  $s_1^A$  is computed according to:

$$s_1^A = t_1^B + \frac{d^{AB}}{c - v_r^{AB}}$$

20 where;

$t_1^B$  is the time of transmission of the signal from clock B according to clock B;

$d^{AB}$  is the distance from clock A to clock B at the time  $t_1^B$ ;

c is the velocity of light in a vacuum;

$v_r^{AB}$  is the radial velocity of clock B relative to clock A at the time  $t_1^B$ ;

25 3. The method of claim 1 wherein clock B is in a GPS satellite and the signal from the satellite has ephemeris data to allow calculation of  $d^{AB}$  and  $v_r^{AB}$ .

4. The method of claim 3 wherein clocks A and C are on the earth.

5. The method of claim 3 wherein clock A is on the earth and clock C is on a satellite and clock C has its position and velocity computed timely for calculation of  $\varepsilon^C$ .

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6. The method of claim 3 wherein clock A is on a satellite and clock C is on a satellite and both clock A and clock C have their position and velocity computed timely for calculation  $\varepsilon^A$  and  $\varepsilon^C$  respectively.

10 7. A method of synchronizing a plurality of clocks at different locations on earth using a clock in a satellite that is in translation relative to the clocks on earth, where an arbitrary one of the clocks on earth is referred to as clock A and an arbitrary other of the clocks on earth is referred to as clock C, and the clock in the satellite is referred to as clock B, and where the process can be used with a single defined clock A, or by

15 designating any clock of the plurality of clocks as clock A, and any other of the clocks of the plurality of clocks as clock B comprising the steps of;

stage 1, at clock A

receiving the signal from clock B;

recording the time  $t_1^A$ , of reception of a specific epoch according to clock

20 A;

recording the time  $t_1^B$ , of transmission of the epoch according to clock B;

determining the location,  $x_1^B, y_1^B, z_1^B$ , and velocity vector  $\bar{v}_1^B$ , of B at the time  $t_1^B$ , of the epoch transmission;

determining the radial component  $v_r^{AB}$  of relative velocity between clock A

25 and clock B;

determining at clock A the propagation time of the signal epoch in traveling from A to B,  $t_{prop}^{BA}$ ;

determining the epoch arrival time  $s^A$ , at clock A;

determining the correction term for clock A,  $\varepsilon^A$ ;

stage 2, at clock B

receiving the signal from clock B;

recording the time  $t_2^C$  of reception of a specific epoch according to clock C;

5 recording the time  $t_2^B$  of transmission of the epoch according to clock B;  
determining the location  $x_2^B, y_2^B, z_2^B$ , and

the velocity vector  $\bar{v}_2^B$  of B at the time  $t_2^B$  of the specific epoch transmission;

10 determining the radial component  $v_r^{CB}$  of relative velocity between clock C and clock B;

determining at clock C the propagation time of the signal epoch in traveling from clock B to clock C,  $t_{prop}^{BC}$ ;

determining the epoch arrival time,  $s_2^C$  at clock C;

determining correction term for clock C,  $\varepsilon^C$ ;

stage 3, at clock C

differencing the correction term  $\varepsilon^C$  and  $\varepsilon^A$  to determine  $\varepsilon^{CA}$ ;

synchronizing clock C to clock A by applying  $\varepsilon^{CA}$  to the unsynchronized reading of clock C.

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8. The method of claim 7 wherein  $s_1^A$  is computed according to:

$$s_1^A = t_1^B + \frac{d^{AB}}{c - v_r^{AB}}$$

where;

$t_1^B$  is the time of transmission of the signal from clock B according to clock B;

25  $d^{AB}$  is the distance from clock A to clock B at the time  $t_1^B$ ;

c is the velocity of light in a vaccum;

$v_r^{AB}$  is the radial velocity of clock B relative to clock A at the time  $t_1^B$ ;

9. The method of claim 7 wherein clock B is in a GPS satellite and the signal from the satellite has ephemeris data to allow calculation of  $d^{AB}$  and  $v_r^{AB}$ .

5 10. The method of claim 7 wherein clocks A and C are on the earth.

11. The method of claim 7 wherein clock A is on the earth and clock C is on a satellite and clock C has its position and velocity computed timely for calculation of  $\varepsilon^C$ .

10 12. The method of claim 7 wherein clock A is on a satellite and clock C is on a satellite and both clock A and clock C have their position and velocity computed timely for calculation  $\varepsilon^A$  and  $\varepsilon^C$  respectively.

13. A method of synchronizing a clock in a satellite to a clock on the earth, comprising the steps of:

transmitting a signal  $S_w$  from a first clock (clock A) at time  $t_1^A$  according to clock A;

recording at clock A the time  $t_1^A$  of transmission of signal  $S_w$ .

recording at the location of the clock in the satellite (clock B) the time  $t_1^B$  that 20 signal  $S_w$  is received by clock B;

at time  $t_1^B$  or at a time known relative to time  $t_1^B$ , transmitting a signal  $S_x$  from the satellite, said signal  $S_x$  containing a message indicating the value of  $t_1^B$ ;

recording at clock A the time  $t_2^A$  that signal  $S_x$  is received by clock A, and recording the value of  $t_1^B$  from the message contained in signal  $S_x$ ;

25 at time  $t_2^A$  or at a time known relative to time  $t_2^A$ , transmitting a signal  $S_y$  from clock A;

receiving the signal at clock B at time  $t_1^B$  according to clock B;

at time  $t_2^B$  or at a time known relative to time  $t_2^B$ , transmitting a signal  $S_z$  from clock B;

recording at clock A the time  $t_3^A$  that signal  $S_z$  is received by clock A;  
determining the characteristic value  $\xi$  of relative motion according to the expression

$$\xi = \left( \frac{t_3^A - t_2^A}{t_2^A - t_1^A} \right)^{\frac{1}{2}};$$

5 obtaining the synchronized time  $s_1^B$  of reception of signal  $S_w$  according to the formula

$$s_1^B = \frac{1}{\xi + 1} (t_2^A + \xi t_1^A);$$

determining a correction term  $\varepsilon^B$ , which is  $s_1^B - t_1^B$ ;

10 sending the value of  $\varepsilon^B$  to the satellite and having the satellite broadcast the value of  $\varepsilon^B$  along with its unsynchronized time  $t^B$ , or sending the value of  $\varepsilon^B$  to the satellite and having the satellite use  $\varepsilon^B$  in conjunction with  $t^B$  to broadcast a synchronized time.

14. A method of synchronizing a clock in a satellite to a clock on the earth, comprising the steps of:

15 transmitting a signal  $S_w$  from a reference clock (clock A) at time  $t_1^A$  according to clock A, said signal  $S_w$  containing a message indicating the value of  $t_1^A$ ;

recording at the location of the clock in the satellite (clock B) the time  $t_1^B$  that signal  $S_w$  is received by clock B, and recording the value of  $t_1^A$  from the message contained in signal  $S_w$ ;

20 at time  $t_1^B$  or at a time known relative to time  $t_1^B$ , transmitting a signal  $S_x$  from the satellite;

recording at clock A the time  $t_2^A$  that signal  $S_x$  is received by clock A;

at time  $t_2^A$  or at a time known relative to time  $t_2^A$ , transmitting a signal  $S_y$  from clock A, said signal  $S_y$  containing a message indicating the value of  $t_2^A$ ;

25 recording at clock B the time  $t_2^B$  that signal  $S_y$  is received by clock B, and recording the value of  $t_2^A$  from the message contained in signal  $S_y$ ;

determining the characteristic value  $\xi$  of relative motion according to the expression

$$\xi = \frac{t_2^B - t_1^B}{t_2^A - t_1^A};$$

5 obtaining the synchronized time  $s_1^B$  of reception of signal  $S_w$  according to the formula

$$s_1^B = \frac{1}{\xi + 1} (t_2^A + \xi t_1^A);$$

determining a correction term  $\varepsilon^B$ , which is  $s_1^B - t_1^B$ ;

10 having the satellite broadcast the value of  $\varepsilon^B$  along with its unsynchronized time  $t^B$ , or sending the value of  $\varepsilon^B$  to the satellite and having the satellite use  $\varepsilon^B$  in conjunction with  $t^B$  to broadcast a synchronized time.